

Case statical

Introduction: Data Analysis: Making Sense of Data

Data

Do Rewards Promote Creativity?

who had not vate speople to be creative a text the possibility of receiving an external reward—like money spraise: fame for a good grade? Or is the personal satisfaction gained from do not of the original satisfaction gained from do not originally work its own reward? Researcher Teresa Amabile designed a study to find out. He is specific research question was! Will competing for a prize improve children's artistic of the control of the c

Belleville Commission of the C

mabile githered some elementary school students to take part in her study. The children were divided into two groups and instructed to make a "silly" collage using materials that were provided. Before they started the children in one group were told that their collages would be judged by experts and that the winners would receive prizes. The children in the other group were told that they would share their collages at an art party. In fact, expert judges rated the creativity of all the collages.

Want to know what happened? By the end of this chapter, you'll have your answer.

• From data analysis to inference

Data analysis



15 countries record hundreds of millions of transactions every week. In all these cases, the data are trying to tell us a story—about U.S. households, objects in space, or Walmart shoppers. To hear what the data are saying, we need to help them speak by organizing, displaying, summarizing, and asking questions. That's data analysis.

Individuals and Variables

Any set of data contains information about some group of individuals. The characteristics we measure on each individual are called variables.

DEFINITION: Individuals and variables

Individuals are the objects described by a set of data. Individuals may be people, animals, or things.

A variable is any characteristic of an individual. A variable can take different values for different individuals.

A high school's student data base, for example, includes data about every currently enrolled student. The students are the *individuals* described by the data set. For each individual, the data contain the values of *variables* such as age, gender, grade point average, homeroom, and grade level. In practice, any set of data is accompanied by background information that helps us understand the data. When you first meet a new data set, ask yourself the following questions:

1. Who are the individuals described by the data? How many individuals are there?

categorical and quantitative data effectively on the AP exam. (people or dwellings) into categories based on location. Some variables—such as gender, race, and occupation—are categorical by nature. Other categorical variables are created by grouping values of a quantitative variable into classes. For instance, we could classify people in a data set by age: 0–9, 10–19, 20–29, and so on. The proper method of analysis for a variable depends on whether it is categorical or quantitative. As a result, it is important to be able to distinguish these two



Census at School

Data, individuals, and variables

types of variables.



New Zealand, South Africa, and the United Kingdom have taken part in the project since 2000. Data from the surveys are available at the project's Web site (www.censusatschool.com). We used the site's "Random Data Selector" to choose 10 Canadian students who completed the survey in a recent year. The table below displays the data.

CensusAtSchool is an international project that collects data about primary and secondary school students using surveys. Hundreds of thousands of students from Australia, Canada,

Province	Gender	Languages spoken	Handed	Height (cm)	Wrist circum. (mm)	Preferred communication	Travel to school (min)
Ontario	Male	1 -	Right	175	175	Internet chat or MSN	25
Alberta	Female	3	Right	147	140	MySpace/Facebook	20
Ontario	Male	1	Right	165	170	Internet chat	4
British Columbia	Female	1	Right	155	145	In person	10
New Brunswick	Male	9	Left	130.5	130	Other	40
Ontario	Male	2	Right	170	16 5	In person	7
Ontario	Male	3	Left	150	100	Internet chat	10
New Brunswick	Male	2	Both	167.5	220	Internet chat	30
	<u>-</u>					- , ,	40

in this example, is a good idea.

egorical), number or languages spoken (quantitative, in whole numbers), dominant hand (categorical), height (quantitative, in centimeters), wrist circumference (quantitative, in millimeters), preferred communication method (categorical), and travel time to school (quantitative, in minutes).

(c) This student lives in Ontario, is male, speaks three languages, is left-handed, is 150 cm tall (about 59 inches), has a wrist circumference of 100 mm (about 4 inches), prefers to communicate via Internet chat, and travels 10 minutes to get to school.



Try Exercise 3

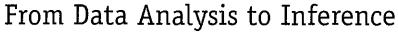
To make life simpler, we sometimes refer to "categorical data" or "quantitative data" instead of identifying the variable as categorical or quantitative. Most data tables follow the format shown in the example—each row is an individual, and each column is a variable. Sometimes the individuals are called *cases*. A variable generally takes values that vary (hence the name "variable"!). Categorical variables sometimes have similar counts in each category and sometimes don't. For instance, we might have expected similar numbers of males and females in the CensusAtSchool data set. But we aren't surprised to see that most students are right-handed. Quantitative variables may take values that are very close together or values that are quite spread out. We call the pattern of variation of a variable its distribution.

DEFINITION: Distribution

The **distribution** of a variable tells us what values the variable takes and how often it takes these values.



Section 1.1 begins by looking at how to describe the distribution of a single categorical variable and then examines relationships between categorical variables. Sections 1.2 and 1.3 and all of Chapter 2 focus on describing the distribution of a quantitative variable. Chapter 3 investigates relationships between two quantitatives.



Inference

Sometimes, we're interested in drawing conclusions that go beyond the data at hand. That's the idea of inference. In the CensusAtSchool example, 7 of the 10 randomly selected Canadian students are right-handed. That's 70% of the *sample*. Can we conclude that 70% of the *population* of Canadian students who participated in CensusAtSchool are right-handed? No. If another random sample of 10 students was selected, the percent who are right-handed would probably not be exactly 70%. Can we at least say that the actual population value is "close" to 70%? That depends on what we mean by "close."

The following Activity gives you an idea of how statistical inference works.

ACTIVITY Hiring discrimination—it just won't fly!

MATERIALS: Deck of cards for each student or pair of students



An airline has just finished training 25 pilots—15 male and 10 female—to become captains. Unfortunately, only eight captain positions are available right now. Airline managers announce that they will use a lottery to determine which pilots will fill the available positions. The names of all 25 pilots will be written on identical slips of paper, which will be placed in a hat, mixed thoroughly, and drawn out one at a time until all eight captains have been identified.

A day later, managers announce the results of the lottery. Of the 8 captains chosen, 5 are female and 3 are male. Some of the male pilots who weren't selected suspect that the lottery was not carried out fairly. One

plot the number of females obtained in each of the five simulation trials on the graph.

- 5. Discuss the results with your classmates. Does it seem believable that airline managers carried out a fair lottery? What advice would you give the male pilot who contacted you?
- 6. Would your advice change if the lottery had chosen 6 female (and 2 male) pilots? Explain.

Our ability to do inference is determined by how the data are produced. Chapter 4 discusses the two primary methods of data production—sampling and experiments—and the types of conclusions that can be drawn from each. As the Activity illustrates, the logic of inference rests on asking, "What are the chances?" *Probability*, the study of chance behavior, is the topic of Chapters 5 through 7. We'll introduce the most common inference techniques in Chapters 8 through 12.



A data set contains information on a number of individuals. Individuals

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In Section 1.1, you'll learn about:

- Bar graphs and pie charts
- Graphs: Good and bad
- Two-way tables and marginal distributions
- Relationships between categorical variables: Conditional distributions
- Organizing a statistical problem
- Simpson's paradox*

The values of a categorical variable are labels for the categories, such as "male" and "female." The distribution of a categorical variable lists the categories and gives either the *count* or the *percent* of individuals who fall in each category. Here's an example.



Radio Station Formats Distribution of a categorical variable

The radio audience rating service Arbitron places the country's 13,838 radio stations into categories that describe the kinds of programs they broadcast. Here are two different tables showing the distribution of station formats:³

Frequer	ncy table
Format	Count of station
Adult contemporary	1,556
Adult standards	1,196
Contemporary hit	569
Country	2,066
News/Talk/Information	2,179
Oldies	1,060
Religious	2,014
1	

Relative from	equency table
Format	Percent of stations
Adult contemporary	11.2
Adult standards	8.6
Contemporary hit	4.1
Country	14.9
News/Talk/Information	15.7
Oldies	7.7
Religious	14.6
Park	6.3

Bar Graphs and Pie Charts

Pie chart Bar graph Columns of numbers take time to read. You can use a pie chart or a bar graph to display the distribution of a categorical variable more vividly. Figure 1.1 illustrates both displays for the distribution of radio stations by format.

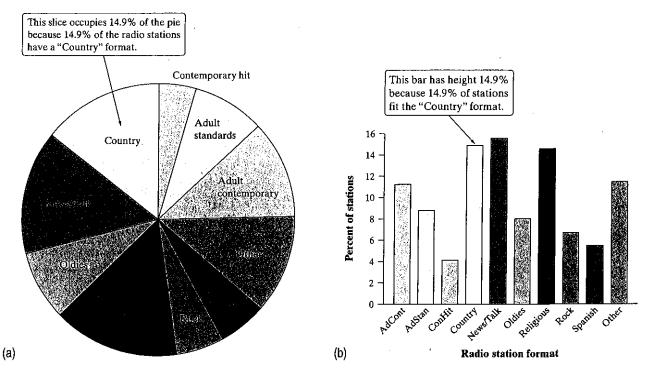


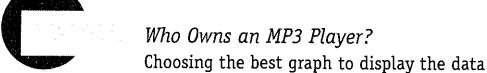
FIGURE 1.1 (a) Pie chart and (b) bar graph of U.S. radio stations by format.



Bar graphs are also called bar charts.

Bar graphs represent each category as a bar. The bar heights show the category counts or percents. Bar graphs are easier to make than pie charts and are also easier to read. To convince yourself, try to use the pie chart in Figure 1.1 to estimate the percent of radio stations that have an "Oldies" format. Now look at the bar graph—it's easy to see that the answer is about 8%.

Bar graphs are also more flexible than pie charts. Both graphs can display the distribution of a categorical variable, but a bar graph can also compare any set of quantities that are measured in the same units.



Portable MP3 music players, such as the Apple iPod, are popular—but not equally popular with people of all ages. Here are the percents of people in various age groups who own a portable MP3 player, according to an Arbitron survey of 1112 randomly selected people.⁴

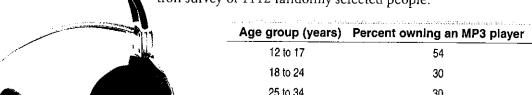


FIGURE 1.2 Bar graph comparing the percents of several age groups who own portable MP3 players.

Graphs: Good and Bad

Bar graphs compare several quantities by comparing the heights of bars that represent the quantities. Our eyes, however, react to the *area* of the bars as well as to their height. When all bars have the same width, the area (width \times height) varies in proportion to the height, and our eyes receive the right impression. When you draw a bar graph, make the bars equally wide. Artistically speaking, bar graphs are a bit dull. It is tempting to replace the bars with pictures for greater eye appeal. Don't do it! The following example shows why.



Who Buys iMacs?

Beware the pictograph!

When Apple, Inc., introduced the iMac, the company wanted to know whether this new computer was expanding Apple's market share. Was the iMac mainly being bought by previous Macintosh owners, or was it being purchased by first-time computer buyers and by previous PC users who were switching over? To find out, Apple hired a firm to conduct a survey of 500 iMac customers. Each customer was categorized as a new computer purchaser, a previous PC owner, or a previous Macintosh owner. The table summarizes the survey results.⁵

Previous ownership	Count	Percent
None	85	17.0

SOLUTION:

- (a) Although the heights of the pictures are accurate, our eyes respond to the area of the pictures. The pictograph makes it seem like the percent of iMac buyers who are former Mac owners is at least ten times higher than either of the other two categories, which isn't the case.
- (b) The bar graph on the right is misleading. By starting the vertical scale at 10 instead of 0, it looks like the percent of iMac buyers who previously owned a PC is less than half the percent who are first-time computer buyers. We get a distorted impression of the relative percents in the three categories.



Try Exercise 17

There are two important lessons to be learned from this example: (1) beware the pictograph, and (2) watch those scales.

Two-Way Tables and Marginal Distributions

We have learned some techniques for analyzing the distribution of a single categorical variable. What do we do when a data set involves two categorical variables? We begin by examining the counts or percents in various categories for one of the variables. Here's an example to show what we mean.



I'm Gonna Be Rich!

Relationship between two categorical variables

A survey of 4826 randomly selected young adults (aged 19 to 25) asked, "What do you think are the chances you will have much more than a middle-class income at age 30?" The table below shows the responses, omitting a few people who refused to respond or who said they were already rich.⁶

How can we best grasp the information contained in the two-way table above? First, look at the distribution of each variable separately. The distribution of a categorical variable says how often each outcome occurred. The "Total" column at the right of the table contains the totals for each of the rows. These row totals give the distribution of opinions about becoming rich in the entire group of 4826 young adults: 194 felt that they had almost no chance, 712 thought they had just some chance, and so on. (If the row and column totals are missing, the first thing to do in studying a two-way table is to calculate them.) The distributions of opinion alone and gender alone are called marginal distributions because they appear at the right and bottom margins of the two-way table.

DEFINITION: Marginal distribution

The **marginal distribution** of one of the categorical variables in a two-way table of counts is the distribution of values of that variable among all individuals described by the table.

Percents are often more informative than counts, especially when we are comparing groups of different sizes. We can display the marginal distribution of opinions in percents by dividing each row total by the table total and converting to a percent. For instance, the percent of these young adults who think they are almost certain to be rich by age 30 is

$$\frac{\text{almost certain total}}{\text{table total}} = \frac{1083}{4826} = 0.224 = 22.4\%$$

Almost certain

FIGURE 1.3 Bar graph showing the marginal distribution of opinion about chance of being rich by age 30.

(b) Figure 1.3 is a bar graph of the distribution of opinion among these young adults. It seems that many young adults are optimistic about their future income. Over 50% of those who responded to the survey felt that they had "a good chance" or were "almost certain" to be rich by



Each marginal distribution from a two-way table is a distribution for a single categorical variable. As we saw earlier, we can use a bar graph or a pie chart to display such a distribution.



age 30.

CHECK YOUR UNDERSTANDING

- 1. Use the data in the two-way table on page 12 to calculate the marginal distribution (in percents) of gender.
- 2. Make a graph to display the marginal distribution. Describe what you see.

Relationships between Categorical Variables: Conditional Distributions

The two-way table contains much more information than the two marginal distributions of opinion alone and gender alone. Marginal distributions tell us nothing about the relationship between two variables. To describe a relationship between two categorical variables, we must calculate some well-chosen percents from the

Almost certain =20.5%EXAMPLE the count of such men by the total number of men, the column total:

A good chance

conditional distribution of opinion among women. See the table in the margin. We use the term "conditional" because this distribution describes only young adults who satisfy the condition that they are female.

DEFINITION: Conditional distribution

A conditional distribution of a variable describes the values of that variable among individuals who have a specific value of another variable. There is a separate conditional distribution for each value of the other variable.

Now let's examine the men's opinions.

I'm Gonna Be Rich!

Calculating a conditional distribution

PROBLEM: Calculate the conditional distribution of opinion among the men.

SOLUTION: To find the percent of men who think they are almost certain to be rich by age 30, divide

$$\frac{\text{men who are almost certain}}{\text{column total}} = \frac{597}{2459} = 24.3\%$$

If we do this for all five entries in the "Male" column, we get the conditional distribution shown in the table.

> Male Response

examples.

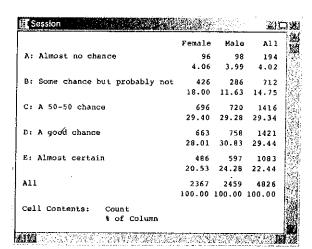


FIGURE 1.4 Minitab output for the two-way table of young adults by gender and chance of being rich, along with each entry as a percent of its column total. The "Female" and "Male" columns give the conditional distributions of opinion for women and men, and the "All" column shows the marginal distribution of opinion for all these young adults.

There are two sets of conditional distributions for any two-way table. So far, we have looked at the conditional distributions of opinion for the two genders. We could also examine the five conditional distributions of gender, one for each of the five opinions, by looking separately at the rows in the original two-way table. For instance, the conditional distribution of gender among those who responded "Almost certain" is

Female

Mala

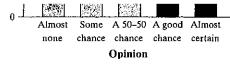


FIGURE 1.5 Bar graph comparing the percents of females among those who hold each opinion about their chance of being rich by age 30.

Almost Some A 50-50 A good Almost none chance chance chance certain

Opinion

FIGURE 1.6 Segmented bar graph showing the conditional distribution of gender for each opinion category.

Segmented bar graph

An alternative to the bar graph in Figure 1.5 is a segmented bar graph, like the one shown in Figure 1.6. For each opinion category, there is a single bar with "segments" that correspond to the different genders. The height of each segment is determined by the percent of young adults having that opinion who were of each gender. We can see the two percents we calculated earlier displayed in the "Almost certain" bar—female 44.9% and male 55.1%. Notice that each bar has a total height of 100%.

THINK ABOUT IT Which conditional distributions should we compare? Our goal all along has been to analyze the relationship between gender and opinion about chances of becoming rich for these young adults. We started by examining the conditional distributions of opinion for males and females. Then we looked at the conditional distributions of gender for each of the five opinion categories. Which of these two gives us the information we want? Here's a hint: think about whether changes in one variable might help explain changes in the other. In this case, it seems reasonable to think that gender might influence young adults' opinions about their chances of getting rich. To see whether the data support this idea, we should compare the conditional distributions of opinion for women and men.



CHECK YOUR UNDERSTANDING

1. Find the conditional distributions of gonder among each of the other four eninion set

EXAMPLE

a graph, perform a calculation, interpret a result, and so on. Real statistics problems don't come with such detailed instructions, however. From now on, you will encounter some examples and exercises that are more realistic. They are marked with the four-step icon. Use the four-step process as a guide to solving these problems, as the following example illustrates.

Women's and Men's Opinions Conditional distributions and relationships



Based on the survey data, can we conclude that young men and women differ in their opinions about the likelihood of future wealth? Give appropriate evidence to support your answer. Follow the four-step process.

A good chance

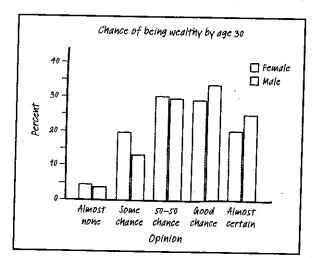


FIGURE 1.7 Side-by-side bar graph comparing the opinions

STATE: What is the relationship between gender and responses to the question "What do you think are the chances you will have much more than a middle-class income at age 30?"

PLAN: We suspect that gender might influence a young adult's opinion about the chance of getting rich. So we'll compare the conditional distributions of response for men alone and for women alone.

Response	Female	Male
Almost no chance	$\frac{96}{2367} = 4.1\%$	$\frac{98}{2459} = 4.0\%$
Some chance	$\frac{426}{2367} = 18.0\%$	$\frac{286}{2459} = 11.6\%$
A 50-50 chance	$\frac{696}{2367} = 29.4\%$	$\frac{720}{2459} = 29.3\%$

 $\frac{758}{2450} = 30.8\%$

Opinion

FIGURE 1.8 Segmented bar

graph comparing the opinions

of males and females.

values of one variable (opinion) tend to occur more or less frequently in combination with specific values of the other variable (gender). Men more often rated their chances of becoming rich in the two highest categories; women said "some chance but probably not" much more frequently. Can we say that there is an association between gender and opinion in the *population* of young adults? Making this determination requires formal inference, which will have to wait a few chapters.

DEFINITION: Association

We say that there is an **association** between two variables if specific values of one variable tend to occur in common with specific values of the other.

There's one caution that we need to offer: even a strong association between two categorical variables can be influenced by other variables lurking in the background. The Data Exploration that follows gives you a chance to explore this idea using a famous (or infamous) data set.

DATA EXPLORATION A Titanic disaster

In 1912 the luxury liner *Titanic*, on its first voyage across the Atlantic, struck an iceberg and sank. Some passengers got off the ship in lifeboats, but many died. The two-way table below gives information about adult passengers who lived and who died, by class of travel.

	Survival S	Status
Class of Travel	Survived	Died
First class	197	122
Second class	94	167

status? Explain.

Simpson's Paradox*

In the most extreme cases, it is possible for an association between two categorical variables to be "reversed" when we consider a third variable. Here is an example that demonstrates the surprises that can await the unsuspecting user of data.



Do Medical Helicopters Save Lives?

Reversing an association

Accident victims are sometimes taken by helicopter from the accident scene to a hospital. Helicopters save time. Do they also save lives? Let's compare the percents of accident victims who die with helicopter evacuation and with the usual transport to a hospital by road. Here are hypothetical data that illustrate a practical difficulty:⁷

	Helicopter	Road
Victim died	64	260
Victim survived	136	840
Total	200	1100

We see that 32% (64 out of 200) of helicopter patients died, but only 24% (260 out of 1100) of the others did. That seems discouraging.

The explanation is that the helicopter is sent mostly to serious accidents, so that the victims transported by helicopter are more often seriously injured. They are more likely to die with or without helicopter evacuation. Here are the same data broken down by the seriousness of the accident:

dents, compared with only 100 of the 1100 road transport patients. So the helicopter carries patients who are more likely to die. The seriousness of the accident was a "lurking variable" that, until we uncovered it, hid the true relationship between survival and mode of transport to a hospital. This example illustrates Simpson's paradox.

DEFINITION: Simpson's paradox

An association between two variables that holds for each individual value of a third variable can be changed or even reversed when the data for all values of the third variable are combined. This reversal is called **Simpson's paradox**.



Summary

- The distribution of a categorical variable lists the categories and gives the count (frequency table) or percent (relative frequency table) of individuals that fall in each category.
- Pie charts and bar graphs display the distribution of a categorical variable. Bar graphs can also compare any set of quantities measured in the same units. When examining any graph, ask yourself, "What do I see?"
- A two-way table of counts organizes data about two categorical variables.

paradox.

1.1 TECHNOLOGY CORNER

Analyzing two-way tables..... page 16



Exercises

9. Cool car colors The most popular colors for cars and light trucks change over time. Silver passed green in 2000 to become the most popular color worldwide, then gave way to shades of white in 2007. Here is the distribution of colors for vehicles sold in North America in 2008.8

Color	Percent of vehicles
White	20
Black	17
Silver	17
Blue	13

10. Spam Email spam is the curse of the Internet. Here is a compilation of the most common types of spam:9

Type of spam	Percent
Adult	19
Financial	20
Health	7
Internet	7
Leisure	6
Products	25
Scams	9

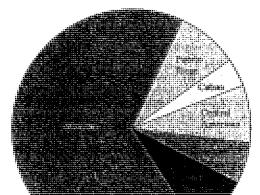
Would it also be correct to make a pie chart?

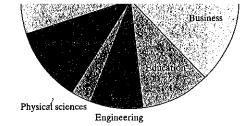
(b) Suggest some possible reasons why there are fewer births on weekends.

(a) Present these data in a well-labeled bar graph.

- 12. Deaths among young people Among persons aged 15 to 24 years in the United States, the leading causes of death and number of deaths in a recent year were as follows: accidents, 15,567; homicide, 5359; suicide, 4139; cancer, 1717; heart disease, 1067; congenital defects, 483.11
 - (a) Make a bar graph to display these data.
 - (b) To make a pie chart, you need one additional piece of information. What is it?
 - Hispanic origins Below is a pie chart prepared by the Census Bureau to show the origin of the more than 43 million Hispanics in the United States in 2006. ¹² About what percent of Hispanics are Mexican? Puerto Rican?

Percent Distribution of Hispanics by Type: 2006

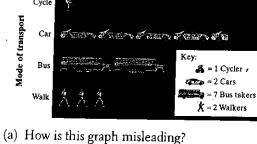




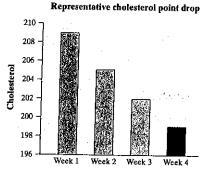
15. Buying music online Young people are more likely
than older folk to buy music online. Here are the
percents of people in several age groups who bought
music online in 2006:14

Age group	Bought music online
12 to 17 years	24%
18 to 24 years	21%
25 to 34 years	· 20%
35 to 44 years	16%
45 to 54 years	10%
55 to 64 years	3%
65 years and over	1%

- (a) Explain why it is *not* correct to use a pie chart to display these data.
- (b) Make a bar graph of the data. Be sure to label your axes and title your graph.
- 16. The audience for movies Here are data on the percent of people in several age groups who attended a movie in the past 12 months:¹⁵

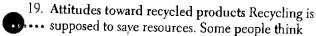


- (b) Make a new graph that isn't misleading.
- 18. Oatmeal and cholesterol Does eating oatmeal reduce cholesterol? An advertisement included the following graph as evidence that the answer is "Yes."



(a) How is this graph misleading?(b) Make a new graph that isu't misleading. What do you conclude about the effect of eating oatmeal ou cholesterol reduction?

- Neither One Both parent parent parents smokes smokes smoke Student does not smoke -1168 1823 1380 Student smokes 188 416 400
 - (a) How many students are described in the two-way table? What percent of these students smoke?(b) Give the marginal distribution of parents' smoking behavior, both in counts and in percents.
- 21. Attitudes toward recycled products Exercise 19 gives data on the opinions of people who have and have not bought coffee filters made from recycled paper. To see the relationship between opinion and experience with the product, find the conditional distributions of opinion (the response variable) for buyers and nonbuyers. What do you conclude?
 - 22. Smoking by students and parents Refer to Exercise 20. Calculate three conditional distributions of students' smoking behavior: one for each of the three parental smoking categories. Describe the relationship between the smoking behaviors of students and their parents in a few sentences.
 - 23. Popular colors—here and there Favorite vehicle colors may differ among countries. The side-by-side bar graph shows data on the most popular colors of cars in 2008 for the United States and Europe. Write a few sentences comparing the two distributions.



they owned, rented, or Respondents were also to an environmental or Club). The two-way tal responses.	asked wh ganizatio	ether they n (like the	i belong Sierra
	Envir	onmental C	iubs
	No-	Yes _	Total
Never üsed	445	212	657
Never üsed Snowmobile renter	445 497	212 77	657 574
110121 4421			

(a) Make a graph to compare colors by vehicle type.(b) Write a few sentences describing what you see.

12

11

Grav

White

Blue

Red

Green

Yellow/gold

Beige/brown

13

25

10

11

Exercises 27 to 32 refer to the following setting. The National Survey of Adolescent Health interviewed several

Multiple choice: Select the best answer.

Follow the four-step process.

the teranonamb between anger and

thousand teens (grades 7 to 12). One question asked was "What do you think are the chances you will be married in the next ten years?" Here is a two-way table of the responses by gender:18

- Female Male 103 119 Almost no chance 171 150 Some chance, but probably not 512 447 A 50-50 chance 710 735 A good chance 756 1174 Almost certain
- (a) 2625. (c) about 46%. (e) None of these. (b) 4877. (d) about 54%.

27. The percent of females among the respondents was

- 7 28. Your percent from the previous exercise is part of(a) the marginal distribution of females.
 - (b) the marginal distribution of gender.(c) the marginal distribution of opinion about marriage.
 - (d) the conditional distribution of gender among adolescents with a given opinion.
 - (a) the conditional distribution of opinion among

- (a) the marginal distribution of geuder.
- (b) the marginal distribution of opinion about marriage.
- (c) the conditional distribution of gender among adolescents with a given opinion.
- (d) the conditional distribution of opinion among adolescents of a given gender.
- (e) the conditional distribution of females among those who said "Almost certain."
- 33. Marginal distributions aren't the whole story Here are the row and column totals for a two-way table with two rows and two columns:

а	b	50
c	ď	50
60	40	100

Find two different sets of counts a, b, c, and d for the body of the table that give these same totals. This shows that the relationship between two variables cannot be obtained from the two individual distributions of the variables.

34.* Baseball paradox Most baseball hitters perform differently against right-handed and left-handed pitching. Consider two players, Joe and Moe, both of whom bat right-handed. The table below records their performance against right-handed and left-handed pitchers:

Player	Pitcher	Hits	At-bats	
Joe	Right	40	100	

enced by the race of the victim. Here are data on 326 cases in which the defendant was convicted of murder: 19

	White De	efendant		Black De	fendant
	White victim	Black victim	•	White victim	Black victim
Death	19	0	Death	11	6
Not	132	9	Not	52	97

- (a) Use these data to make a two-way table of defendant's race (white or black) versus death penalty (yes or no).
- (b) Show that Simpson's paradox holds: a higher percent of white defendants are sentenced to death overall, but for both black and white victims a higher percent of black defendants are sentenced to death.
- (c) Use the data to explain why the paradox holds in language that a judge could understand..
- 36. Fuel economy (Introduction) Here is a small part of a data set that describes the fuel economy (in miles per gallon) of model year 2009 motor vehicles:

Make and model	Vehicle type	Transmis- sion type	Number of cylinders	City mpg	Highway mpg
Aston Martin Vantage	Two-seater	Manual	8	12	19
Honda Civic	Subcom- pact	Automatic	4	25	36
Toyota Prius	Midsize	Automatic	4	48	45

 Describing shape data. • Comparing distributions Stemplots Histograms • Using histograms wisely Dotplot EXAMPLE

tion, we present several types of graphs that can be used to display quantitative data.

Dotplots

One of the simplest graphs to construct and interpret is a dotplot. Each data value is shown as a dot above its location on a number line. We'll show how to make a dotplot using some sports data.

Gooooaaaaallllll!

How to make a dotplot

How good was the 2004 U.S. women's soccer team? With players like Brandi Chastain, Mia Hamm, and Briana Scurry, the team put on an impressive showing en route to winning the gold medal at the 2004 Olympics in Athens. Here are data on the number of goals scored by the team in 34 games played during the 2004 season:²⁰

3 0 2 7 8 2 4 3 5 1 1 4 5 3 1 1 3 3 2 1 2 2 2 4 3 5 6 1 5 5 1 1

Here are the steps in making a dotplot:

- Draw a horizontal axis (a number line) and label it with the variable name. In this case, the variable is number of goals scored.
- Scale the axis. Start by looking at the minimum and maximum values of the variable. For these data, the minimum number of goals scored was 0, and the maximum was 8. So we mark our scale from 0 to 8, with tick marks

We'll learn more formal ways of describing shape, center, and spread and identifying outliers shortly. For now, let's use our informal understanding of these ideas to examine the graph in Figure 1.9. Shape: The dotplot has a peak at 1. This indicates that the team's most frequent Mode number of goals scored in games that season (known as the mode) was 1. In most of its games, the U.S. women's soccer team scored between I and 5 goals. How-

ever, the distribution has a long tail to the right. (Later, we will describe the shape of Figure 1.9 as skewed to the right.) Center: We can describe the center by finding a value that divides the observations so that about half take larger values and about half take smaller values. This value is called the median of the distribution. In Figure 1.9, the median is 3. That is, in a typical game during the 2004 season, the U.S. women's soccer team scored about 3 goals. Of course, we could also summarize the center of the distribution

by calculating the average (mean) number of goals scored per game. For the 2004 season, the team's mean was 3.06 goals. Spread: The spread of a distribution tells us how much variability there is in the data. One way to describe the variability is to give the smallest and largest values.

The spread in Figure 1.9 is from 0 goals to 8 goals scored. Alternatively, we can compute the range of the distribution by subtracting the smallest value from the largest value. For these data, the range is 8 - 0 = 8 goals.

When describing a distribution Outliers: Was the game in which the women's team scored 8 goals an outlier? of quantitative data, don't forget How about the team's 7-goal game? These values differ somewhat from the overall your SOCS (shape, outliers, pattern. However, they don't clearly stand apart from the rest of the distribution. For now, let's agree to call attention only to potential outliers that suggest something special about an observation. In Section 1.3, we'll establish a procedure for determining whether a particular data value is an outlier.

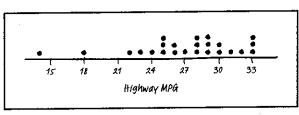
Range

center, spread)!

Delines Amage Rolls Royce Phantom 18 Kia Optima BMW 528! Saturn Aura Lexus GS 350 26 **Buick Lacrosse** Toyota Camry 31 Lincoln MKZ 28 25 Cadillac CTS 29 Volkswagen Passat Mazda 6 Chevrolet Malibu 33 25 Volvo S80 Mercedes-Benz E350 24 30 Chrysler Sebring -Source: 2009 Fuel Economy Guide, from the U.S. Environmental Protection Agency's Web site at www.fueleconomy.gov.

ource: 2009 Paet Economy

Here is a dotplot of the data:



PROBLEM: Describe the shape, center, and spread of the distribution. Are there any outliers? SOLUTION: Don't forget your SOCS (shape, outliers, center, spread)! Shape: In the dotplot, we can see three clusters of values: cars that get around 25 mpg, cars that get about 28 to 30 mpg, and cars that get around 33 mpg. We can also see large gaps between the Acura RL at 22 mpg, the Rolls Royce Phantom at 18 mpg, and the Bentley Arnage at 14 mpg. Center: The median is 28. So a "typical" model year 2009 midsize car got about 28 miles per gallon on the highway. Spread: The highest value is 33 mpg and the lowest value is 14 mpg. The range is 33 — 14 = 19 mpg. Outliers: We see two midsize cars with unusually low gas mileage ratings—the Bentley Arnage (14 mpg) and the Rolls Royce Phantom (18 mpg). These cars are potential outliers.

Describing Shape

When you describe a distribution's shape, concentrate on the main features. Look

For Practice Try Exercise 39





Die Rolls and Quiz Scores

Describing shape

Figure 1.10 displays dotplots for two different sets of quantitative data. Let's practice describing the shapes of these distributions. Figure 1.10(a) shows the results of rolling a pair of fair, six-sided dice and finding the sum of the up-faces 100 times. This distribution is roughly symmetric. The dotplot in Figure 1.10(b) shows the scores on an AP Statistics class's first quiz. This distribution is skewed to the left.

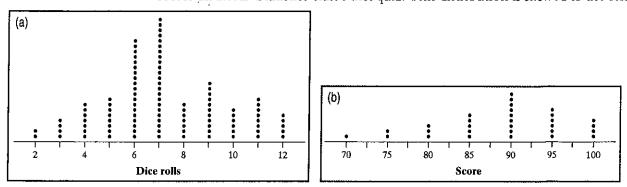


FIGURE 1.10 Dotplots displaying different shapes: (a) roughly symmetric; (b) skewed to the left.



Unimodal

Although the dotplots in the previous example have different shapes, they do have something in common. Both are unimodal, that is, they have a single peak: the graph of dice rolls at 7 and the graph of quiz scores at 90. (We don't count minor ups and downs in a graph, like the "bumps" at 9 and 11 in the dice rolls dotplot, as "peaks.") Figure 1.11 is a dotplot of the duration (in minutes) of 220 eruptions of the Old Faithful geyser. We would describe this distribution's shape

1.5 2.0 2.5 3.0 3.5 4.0 4.5 5.0 Duration (minutes)

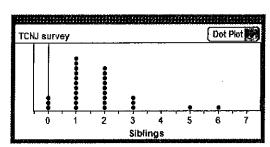
eruptions. This graph has a bimodal shape.

strong right-skew. Many distributions have irregular shapes that are neither symmetric nor skewed. Some data show other patterns, such as the two peaks in Figure 1.11. Use your eyes, describe the pattern you see, and then try to explain the pattern.



CHECK YOUR UNDERSTANDING

The Fathom dotplot displays data on the number of siblings reported by each student in a statistics class.

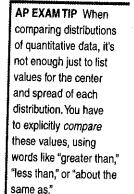


- 1. Describe the shape of the distribution.
- 2. Describe the center of the distribution.
- 3. Describe the spread of the distribution.
- 4. Identify any potential outliers.



SOLUTION: Don't forget your SOCS! Shape: The distribution of household size for the U.K. sample is roughly symmetric and unimodal, while the distribution for the South Africa sample is skewed to the right and unimodal. Center: Household sizes for the South African students tended to be larger than for the U.K. students. The median household sizes for the two groups are 6 people and 4 people, respectively. Spread: There is more variability (greater spread) in the household sizes for the South African students than for the U.K. students. The range for the South African data is 26-3=23 people, while the range for the U.K. data is 6-2=4 people. Outliers: There don't appear to be any potential outliers in the U.K. distribution. The South African distribution has two potential outliers in the right tail of the distribution—students who reported living in households with 15 and 26 people. (The U.K. households with 2 people actually will be classified as outliers when we introduce a procedure in the next section.)

South Africa



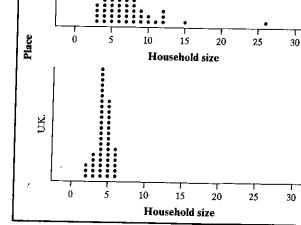


FIGURE 1.12 Dotplot of household size for random samples of 50 students from the United Kingdom and South Africa.

Making a stemplot

How many pairs of shoes does a typical teenager have? To find out, a group of AP Statistics students conducted a survey. They selected a random sample of 20 female students from their school. Then they recorded the number of pairs of shoes that each respondent reported having. Here are the data:

50	26	26	31	.57	19	24	22	23	38
13	50	13	34	23	30	49	13	15	51

Here are the steps in making a stemplot. Figure 1.13 displays the process.

• Separate each observation into a stem, consisting of all but the final digit, and a leaf, the final digit. Write the stems in a vertical column with the smallest at the top, and draw a vertical line at the right of this column.

Do not skip any stems, even if there is no data value for a particular stem. For these data, the tens digits are the stems, and the ones digits are the leaves. The stems run from 1 to 5.

- Write each leaf in the row to the right of its stem. For example, the female student with 50 pairs of shoes would have stem 5 and leaf 0, while the student with 31 pairs of shoes would have stem 3 and leaf 1.
- Arrange the leaves in increasing order out from the stem.
- Provide a key that explains in context what the stems and leaves represent.

with the

| 1 | 93335 | 1 | 33359 | Key: 4|9 represents a female student who reported having 49 pairs of shoes. | Stems | Add leaves | Order leaves | Add a key |

FIGURE 1.13 Making a stemplot of the shoe data. (1) Write the stems. (2) Go through the data and write each leaf on the proper stem. (3) Arrange the leaves on each stem in order out from the stem. (4) Add a key.

The AP Statistics students in the previous example also collected data from a

In Figure 1.14(a), the values from 0 to 9 are placed on the "0" stem. Figure 1.14(b) shows another stemplot of the same data. This time, values having leaves 0 through 4 are placed on one stem, while values ending in 5 through 9 are placed on another stem. Now we can see the single peak, the cluster of values between 4

FIGURE 1.14 Two stemplots showing the male shoe data. Figure 1.14(b) improves on the stemplot of Figure 1.14(a) by splitting stems.

FIGURE 1.15 Back-to-back stemplot comparing numbers of pairs of shoes for male and female students at a school.

What if we want to compare the number of pairs of shoes that males and females have? That calls for a back-to-back stemplot with common stems. The leaves on each side are ordered out from the common stem. Figure 1.15 is a back-to-back stemplot for the male and female shoe data. Note that we have used the split stems from Figure 1.14(b) as the common stems. The values on the right are the male data from Figure 1.14(b). The values on the left are the female data, ordered out from the stem from right to left. We'll ask you to compare these two distributions shortly.

Here are a few tips to consider before making a stemplot:

and 14, and the large gap between 22 and 35 more clearly.

- Stemplots do not work well for large data sets, where each stem must hold a large number of leaves.
- There is no magic number of stems to use, but five is a good minimum. Too few or too many stems will make it difficult to see the distribution's shape.
- If you split stems, be sure that each stem is assigned an equal number of possible leaf digits (two stems, each with five possible leaves; or five stems, each with two possible leaves).
- Instead of rounding, you can You can get more flexibility by rounding the data so that the final digit after also truncate (remove one or rounding is suitable as a leaf. Do this when the data have too many digits. For more digits) when data have too many digits. The teacher's example, in reporting teachers' calories using all 5 11 in 66

Back-to-back stemplot



DIO IEPIESEINO A STATE

Quantitative variables often take many values. A graph of the distribution is clearer if nearby values are grouped together. The most common graph of the distribution of one quantitative variable is a histogram. Let's look at how to make a histogram using data on foreign-born residents in the United States.

Foreign-Born Residents

Making a histogram

What percent of your home state's residents were born outside the United States? The country as a whole has 12.5% foreign-born residents, but the states vary from 1.2% in West Virginia to 27.2% in California. The table below presents the data for all 50 states. The *individuals* in this data set are the states. The *variable* is the percent of a state's residents who are foreign-born. It's much easier to see from a graph than from the table how your state compares with other states.

State	Percent	State	Percent	State	Percent
Alabama	2.8	Louisiana	2.9	Ohio	3.6
Alaska	7.0	Maine	3.2	Oklahoma	4.9
Arizona	15.1	Maryland	12.2	Oregon	9.7
Arkansas	3.8	Massachusetts	14.1	Pennsylvania	5.1
California	27.2	Michigan	5.9	Rhode Island	12.6
Colorado	10.3	Minnesota	6.6	South Carolina	4.1
Connecticut	12.9	Mississippi	1.8	South Dakota	2.2
Delaware	8.1	Missouri	3.3	Tennessee	3.9
Florida	18.9	Montana	1.9	Texas	15.9
Georgia	9.2	Nebraska	5.6	Utah	8.3
Hawali	16.3	Nevada	19.1	Vermont	3.9
ldaha .	5.6	Now Hampahire	· · · · · ·	Virginia	40.4

	Frequer	icy table
	Class	Count
	0 to < 5	20
Notice that the frequen-	5 to < 10	13
cies add to 50, the number of individuals	10 to < 15	9
states) in the data, and	15 to < 20	5
hat the relative frequen-	20 to < 25	2
ies add to 100%.	⁴ 25 to < 30	1
	Total	50
	• Label and scale you with the variable who	er axes and drav

[2]杨俊的《说话》、《2] 本自《文学》、《李成学》、《文学》、《文学》、《文学》、《文学》、《

 Relative frequency table

 Class
 Percent

 0 to < 5</td>
 40

 5 to < 10</td>
 26

 10 to < 15</td>
 18

 15 to < 20</td>
 10

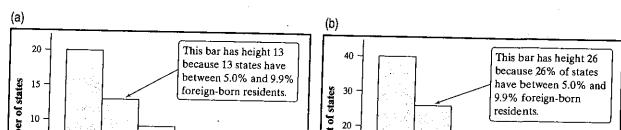
 20 to < 25</td>
 4

 25 to < 30</td>
 2

 Total
 100

• Label and scale your axes and draw the histogram. Label the horizontal axis with the variable whose distribution you are displaying. That's the percent of a state's residents who are foreign-born. The scale on the horizontal axis runs from 0 to 30 because that is the span of the classes we chose. The vertical axis contains the scale of counts or percents. Each bar represents a class. The base of the bar covers the class, and the bar height is the class frequency or relative frequency. Draw the bars with no horizontal space between them unless a class is empty, so that its bar has height zero.

Figure 1.16(a) shows a completed frequency histogram; Figure 1.16(b) shows a completed relative frequency histogram. The two graphs look identical except for the vertical scales.



Center: From the graph, we see that the midpoint (median) would fall somewhere in the 5.0% to 9.9% class. Remember that we're looking for the value having 25 states with smaller percents foreign-born and 25 with larger. (Arranging the observations from the table in order of size shows that the median is 6.1%.)

Spread: The histogram shows that the percent of foreign-born residents in the states varies from less than 5% to over 25%. (Using the data in the table, we see that the range is 27.2% - 1.2% = 26.0%.)

Outliers: We don't see any observations outside the overall single-peaked, right-skewed pattern of the distribution.

Figure 1.17 shows (a) a frequency histogram and (b) a relative frequency histogram of the same distribution, with classes half as wide. The new classes are 0–2.4, 2.5–4.9, etc. Now California, at 27.2%, stands out as a potential outlier in the right tail. The choice of classes in a histogram can influence the appearance of a distribution. Histograms with more classes show more detail but may have a less clear pattern.

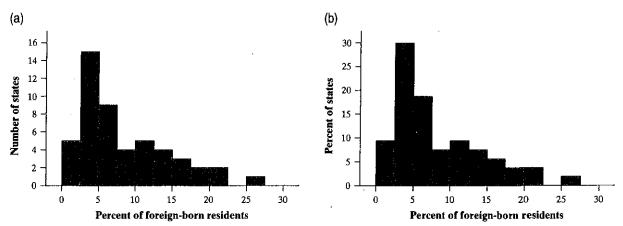
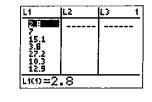
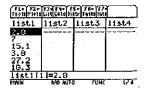


FIGURE 1.17 (a) Frequency histogram and (b) relative frequency histogram of the distribution of the



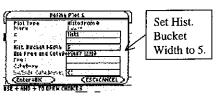


Setup...

[F1] to define.

- 2. Set up a histogram in the Statistics Plots menu.
- Press 2nd Y = (STAT PLOT). • Press F2 and choose 1:Plot
 - Press ENTER or 1 to go into Plot1.





• Press F5 (ZoomData).

• With Plot1 highlighted, press

- Adjust the settings as shown. Adjust the settings as shown.
- 3. Use ZoomStat (ZoomData on the TI-89) to let the calculator choose classes and make a histogram.
 - Press ZOOM and choose
 - 9:ZoomStat.

Note the calculator's

 Press TRACE and I ▶ to exam-• Press F3 (Trace) and ■ ▶ to examine the classes. ine the classes.

unusual choice of classes.

PEXAMTIP If you're sked to make a graph on a free-response question, e sure to label and scale our axes. Unless your alculator shows labels and saling, don't just transfer calculator screen shot to our paper.

Here are some important things to consider when you are constructing a histogram:

- Our eyes respond to the area of the bars in a histogram, so be sure to choose classes that are all the same width. Then area is determined by height, and all classes are fairly represented.
- There is no one right choice of the classes in a histogram. Too few classes will give a "skyscraper" graph, with all values in a few classes with tall bars. Too many will produce a "pancake" graph, with most classes having one or no observations. Neither choice will give a good picture of the shape of the distribution. Five classes is a good minimum.

CHECK YOUR UNDERSTANDING

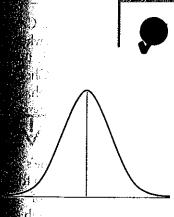
Many people believe that the distribution of IQ scores follows a "bell curve," like the one shown in the margin. But is this really how such scores are distributed? The IQ scores of 60 fifth-grade students chosen at random from one school are shown below.²²

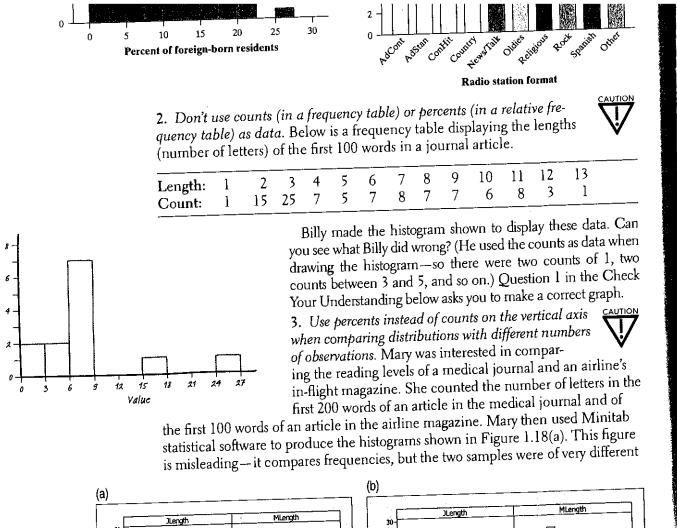
145	139	126	122	125	130	96	110	118	118
101	142	134	124	112	109	134	113	81	113
123	94	100	136	109	131	117	110	127	124
106	124	115	133	116	102	127	117	109	137
117	90	103	114	139	101	122	105	97	89
102	108	110	128	114	112	114	102	82	101

- 1. Construct a histogram that displays the distribution of IQ scores effectively.
- 2. Describe what you see. Is the distribution bell-shaped?

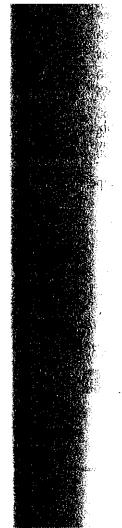
Using Histograms Wisely

We offer several cautions based on common mistakes students make when using

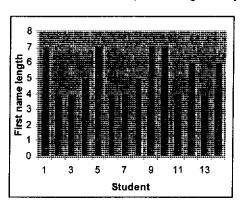




Count



entered into the spreadsheet. It is not a very meaningful display of the data.

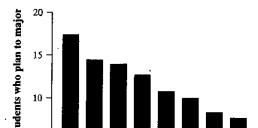




CHECK YOUR UNDERSTANDING

- 1. Draw a correct histogram to replace Billy's graph of the word length data from Caution 2.
- 2. Draw a more meaningful graph of the first-name length data from Caution 4.

Questions 3 and 4 relate to the following setting. About 1.6 million first-year students enroll in colleges and universities each year. What do they plan to study? The graph displays data on the percents of first-year students who plan to major in several discipline areas.²³



of values in equal-width classes.

When examining any graph, look for an overall pattern and for metable

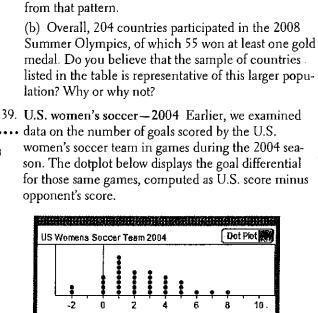
- When examining any graph, look for an overall pattern and for notable departures from that pattern. Shape, center, and spread describe the overall pattern of the distribution of a quantitative variable. Ontliers are observations that lie outside the overall pattern of a distribution. Always look for outliers and try to explain them. Don't forget your SOCS!
- Some distributions have simple shapes, such as **symmetric** or **skewed**. The number of **modes** (major peaks) is another aspect of overall shape. Not all distributions have a simple overall shape, especially when there are few observations.
- When comparing distributions of quantitative data, be sure to discuss shape, center, spread, and possible outliers.
- Remember: histograms are for quantitative data; bar graphs are for categorical data. Also, be sure to use relative frequency histograms when comparing data sets of different sizes.

1.2 TECHNOLOGY CORNER

Histograms on the calculator......page 38

ร 🌣 🌣 🌣 🌣 ซ ซ ซ ซ ซ ซ ซ TI-Nspire instructions in Appendix B





Kazakhstan

Czech Republic

Denmark

Latvia

Hungary

Sweden

Uruguay

(a) Make a dotplot to display these data. Describe the

overall pattern of the distribution and any deviations

United States

36

pg 32

Armenia

India

Georgia

Kyrgyzstan

Costa Rica

Uzbekistan

Brazil

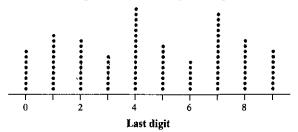
Netherlands

(a) Sketch a dotplot for a distribution that is skewed to the left.(b) Suppose that you and your friends emptied your

41. Dates on coins

pockets of coins and recorded the year marked on each coin. The distribution of dates would be skewed to the left. Explain why.

42. Phone numbers The dotplot below displays the last digit of 100 phone numbers chosen at random from a phone book. Describe the shape of the distribution. Does this shape make sense to you? Explain.

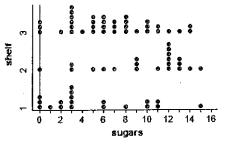


43. Creative writing The chapter-opening Case Study described research by Teresa Amabile investigating whether external rewards would promote creativity in children's artwork. Dr. Amabile conducted another study involving college students, who were divided into two groups using a chance process (like drawing names from a hat). The students in one group were given a list of statements about external reasons

(E) for writing, such as public recognition, making money, or pleasing their parents. Students in the other group were given a list of statements about internal

44. Healthy cereal? Researchers collected data on 77 brands of cereal at a local supermarket. 25 For each brand, the sugar content (grams per serving) and the shelf in the store on which the cereal was located (1 = bottom, 2 = middle, 3 = top) were recorded. A dotplot of the data is shown below. Compare the

(1 = bottom, 2 = middle, 3 = top) were recorded. A dotplot of the data is shown below. Compare the three distributions. Critics claim that supermarkets tend to put sugary kids' cereals on lower shelves, where the kids can see them. Do the data from this study support this claim?



- 45. Where do the young live? Below is a stemplot of the percent of residents aged 25 to 34 in each of the 50 states. As in the stemplot for older residents (page 35), the stems are whole percents, and the leaves are tenths of a percent. This time, each stem has been split in two,

4 | 33
4 | 77

(a) Why did we split stems?

(b) Give an appropriate key for this graph.

(c) Describe the shape, center, and spread of the distribution. Compare the caffeine content of these drinks with the USFDA's limit.

55667778888899

556 033344

113

55567778

47. El Niño and the monsoon It appears that El Niño, the periodic warming of the Pacific Ocean west of South America, affects the monsoon rains that are essential for agriculture in India. Here are the monsoon rains (in millimeters) for the 23 strong El Niño years between 1871 and 2004:²⁶

(a) To make a stemplot of these rainfall amounts, round the data to the nearest 10, so that stems are hundreds of millimeters and leaves are tens of millimeters. Make two stemplots, with and without split-

628 669 740 651 710 736 717 698 653 604 781 784 790 811 830 858 858 896 806 790 792 957 872

- (b) Describe the shape, center, and spread of the distribution.(c) The average monsoon rainfall for all years from
- 1871 to 2004 is about 850 millimeters. What effect

ting the stems. Which plot do you prefer?

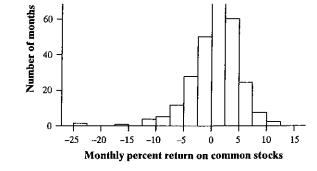
minutes they studied on a typical weeknight. Here are the responses of random samples of 30 women and 30 men from the class:

37												
÷			Womer	1		Men						
	180	120	180	360	240	90	120	30	90	200		
	120	180	120	240	170	90	45	30	120	75		
	150	120	180	180	150	150	120	60	240	300		
	200	150	180	150	180	240	60	120	60	30		
	120	60	-120	180	180	30	230	120	95	150		
	90	240	180	115	120	0	200	120	120	180		

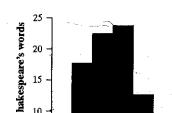
- (a) Examine the data. Why are you not surprised that most responses are multiples of 10 minutes? Are there any responses you consider suspicious?
- (b) Make a back-to-back stemplot to compare the two samples. Does it appear that women study more than men (or at least claim that they do)? Justify your answer.
- 50. Basketball playoffs Here are the scores of games played in the California Division I-AAA high school basketball playoffs:²⁷

71-38	52 -4 7	55-53	76-65	77-63	65-63	68-54	64-62
87-47	64-56	78-64	58-51	91-74	71-41	67-62	106-46

On the same day, the final scores of games in Division V-AA were



- (a) Ignoring the outliers, describe the overall shape of the distribution of monthly returns.
- (b) What is the approximate center of this distribution?
- (c) Approximately what were the smallest and largest monthly returns, leaving out the outliers?
- (d) A return less than zero means that stocks lost value in that month. About what percent of all months had returns less than zero?
- 52. Shakespeare The histogram below shows the distribution of lengths of words used in Shakespeare's plays.²⁹ Describe the shape, center, and spread of this distribution.



FL .	25.9	ΜI	17.6	ľX	24.6		1	Moroc	00		1.4	Т	hailan	d		3.3	
GA	27.3	NE	17.7	UT	20.8		1	Myann	ıar		0.2	Ti	ırkey			3.0	
Hi	25.5	NV	24.2	VT	21.2		١	Vepai			0.1	U.	kraine	!		6.3	
ID	20.1	NH	24.6	VA	26.9		N	Vigeria			0.4	Uı	nited F	Kingdo	om	8.8	
IL	27.9	NJ	29.1	WA	25.2		F	akista	n		0.8	Ur	nited S	States		19.6	
IN	22.3	NM	20.9	WV	25.6		F	eru			1.0	Uz	zbekis	tan		4.2	
IA	18.2	NY	30.9	Wi	20.8		Р	hilippi	nes		0.9		nezue			5.4	
KS	18.5	NC	23.4	WY	17.9		Р	oland			7.8	Vie	etnam			1.0	
KY	22.4	ND	15.5	DC	29.2		_										
 the first class is 14 to 16 minutes, the second is 16 to 18 minutes, and so on. (b) The shape of the distribution is a bit irregular. Is it closer to symmetric or skewed? About where is the center of the data? What is the spread in terms of the smallest and largest values? Are there any outliers?						adm 40 47 52 47	26 19 25 35	39 26 35 48	on to 44 14 35 35 22	42 34 33 33	18 15 29	25 44 34	eir so 43 40 41	6 46 38 49	3 3 1 9 2 8	19 46 52	
54. Carbon dioxide emissions Burning fuels in power plants and motor vehicles emits carbon dioxide (CO ₂), which contributes to global warming. The table below displays CO ₂ emissions per person from countries with populations of at least 20 million. ³¹ (a) Make a histogram of the data using classes of					 47 35 48 22 33 41 51 27 14 54 45 Make a histogram to display the data. Write a paragraph describing the distribution of DRP scores. 56. Drive time Professor Moore, who lives a few miles outside a college town, records the time he takes to drive to the college each morning. Here are the times 												
width 2, starting at 0. (b) Describe the shape, center, and spread of the distribution. Which countries are outliers?						8.25	(in m	inute	es) to	r 42 d 	conse	cutiv	e we	ekda	ays:		
			xide emissions perso			9.00 8.33	8.50 7.83 10.17	9.00 7.92	7.75 8.58	7.9 7.8	2 8.0 3 8.4	00 8. F2 7.	08 8 75 7	3. 4 2 7.42	8.75 6.75	8.08	–

data.

Chest size	Count	Chest size	Count
33	3	41	934
34	18	42	658
35	81	43	370
36	185	44	92
37	420	4 5 ;	50
38	749	46	21
39	1073	47	4
40	1079	48	1

(a) Make a histogram.

chest measurements distribution. Why might this information be useful?

(b) Describe the shape, center, and spread of the

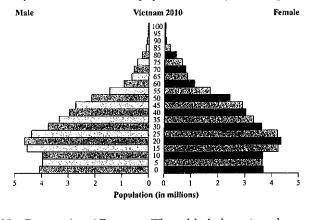
Source: Online Data and Story Library (DASL).

59. Paying for championships Does paying high salaries lead to more victories in professional sports? The New York Yankees have long been known for having Major League Baseball's highest team payroll. And over the years, the team has won many championships. This strategy didn't pay off in 2008, when the Philadelphia Phillies won the World Series. Maybe the Yankees didn't spend enough money that year. The graph below shows histograms of the salary distributions for the two teams during the 2008 season. Why can't you use this graph to effectively compare the team payrolls?

STATE LANGE THE PROPERTY OF TH

- 61. Birth months Imagine asking a random sample of 60 students from your school about their birth months. Draw a plausible graph of the distribution of birth months. (*Hint:* Should you use a bar graph or a histogram?)
- 62. Die rolls Imagine rolling a fair, six-sided die 60 times. Draw a plausible graph of the distribution of die rolls. (*Hint*: Should you use a bar graph or a histogram?)
- 63. Who makes more? A manufacturing company is reviewing the salaries of its full-time employees below the executive level at a large plant. The clerical staff is almost entirely female, while a majority of the production workers and technical staff are male. As a result, the distributions of salaries for male and female employees may be quite different. The table below gives the frequencies and relative frequencies for women and men.

•		-				
	Wom	en	Men			
Salary (\$1000)	Number	%	Number	%		
10–15	89	11.8	26	1.1		
15–20	192	25.4	221	9.0		
20-25	236	31.2	677	27.6		
25-30	111	14.7	823	33.6		
30-35	86	11.4	365	14.9		
35-40	25	3.3	182	7.4		



65. Comparing AP scores The table below gives the distribution of grades earned by students taking the AP Calculus AB and AP Statistics exams in 2009.34

Grade

				*		
	No. of exams	5	4	3	2	1
Calculus AB	230,588	52,921	4 3 ,140	41,204	35,843	57,48
Statistics	116,876	14,353	26,050	28,276	22,283	25,91

- (a) Make an appropriate graphical display to compare the grade distributions for AP Calculus AB and AP Statistics.
- (b) Write a few sentences comparing the two distributions of exam grades.
- 66. Population pyramids Refer to Exercise 64. Here is a graph of the projected population distribution for China in the year 2050. Describe what the graph suggests about China's future population. Be specific.

Explain your reasoning. (b) (a)

ine ngure below snows histograms of the student

responses, in scrambled order and without scale markings. Which histogram goes with each variable?

you plan to make in a study of each of the following issues at your school? Explain your choices.

68. Choose a graph What type of graph or graphs would

(d)

(c)

per day?

- (a) Which radio stations are most popular with students?
- (b) How many hours per week do students study? (c) How many calories do students consume

Multiple choice: Select the heet answer for Francisco 69

71. You look at real estate ads for houses in Naples, Florida. There are many houses ranging from \$200,000 to \$500,000 in price. The few houses on the water, however, have prices up to \$15 million. The distribution of house prices will be

(a) skewed to the left.

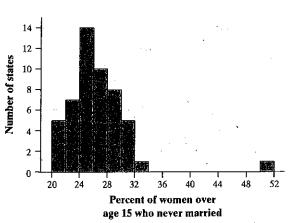
(b) roughly symmetric.

(c) skewed to the right.

(d) unimodal.

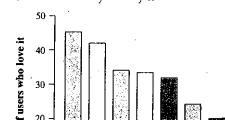
(e) too high.

Exercises 72 to 74 refer to the following setting. The histogram below shows the distribution of the percents of women aged 15 and over who have never married in each of the 50 states and the District of Columbia.



23,854,494 Ramirez. Dodgers Outfielder Manny Santana. Mets Pitcher 6-0 18,876,139 Johan Zambrano, Cubs Pitcher 27 6-5 255 18,750,000 Carlos Mariners Outfielder 18,000,000 Suzuki, 5-11 Ichiro

- (a) What individuals does this data set describe?(b) In addition to the player's name, how many variables does the data set contain? Which of these variables are categorical and which are quantitative?(c) What do you think are the units of measurement
- (c) What do you think are the units of measurement for each of the quantitative variables?
- 76. I love my iPod! (1.1) The rating service Arbitron asked adults who used several high-tech devices and services whether they "loved" using them. Below is a graph of the percents who said they did. 35
 - (a) Summarize what this graph tells you in a sentence or two.
 - (b) Would it be appropriate to make a pie chart of these data? Why or why not?





In Section 1.3, you'll learn about:

- Measuring center: The mean
- Measuring center: The median
- Comparing the mean and the median
- Measuring spread: The interquartile range (IQR)
- Identifying outliers
- The five-number summary and boxplots
- Measuring spread: The standard deviation
- Numerical summaries with technology
- Choosing measures of

Describing Quantitative Data with Numbers

How long do people spend traveling to work? The answer may depend on where they live. Here are the travel times in minutes for 15 workers in North Carolina, chosen at random by the Census Bureau:³⁷

30 20 10 40 25 20 10 60 15 40 5 30 12 10 10

We aren't surprised that most people estimate their travel time in multiples of 5 minutes. Here is a stemplot of these data:

0	5	
1	000025	
2	005	Key: 2 5 is a NC
3	00	worker who travels 25
4	00	minutes to work.
5		
6	l n	

The distribution is single-peaked and right-skewed. The longest travel time (60 minutes) may be an outlier. Our goal in this section is to describe the center and spread of this and other distributions of quantitative data with numbers.

Measuring Center: The Mean

Actually, the notation \overline{x} refers to the mean of a sample. Most of the time, the data we'll encounter can be thought of as a sample from some larger population. When we need to refer to a population mean, we'll use the symbol μ (Greek letter mu, pronounced "mew"). If you have the entire population of data available, then you calculate μ in just the way you'd expect: add the values of all the observations, and divide by the number of observations.



Travel Times to Work in North Carolina Calculating the mean

Refer to the data on travel times to work for the sample of 15 North Carolinians.

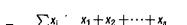
0 5 1 000025 2 005 3 00 4 00 5 6 0	Key: 2 5 is a NC worker who travels 25 minutes to work.
--	---

PROBLEM:

- (a) Find the mean travel time for all 15 workers.
- (b) Calculate the mean again, this time excluding the person who reported a 60-minute travel time to work. What do you notice?

SOLUTION:

(a) The mean travel time for the sample of 15 North Carolina workers is





IL

1 3 4 4 4 5 7 8

What's the mean number of pets for this group of children? It's

$$\overline{x} = \frac{\text{sum of observations}}{n} = \frac{1+3+4+4+4+5+7+8+9}{9} = 5 \text{ pets}$$

But what does that number tell us? Here's one way to look at it: if every child in the group had the same number of pets, each would have 5 pets. In other words, the mean is the "fair share" value.

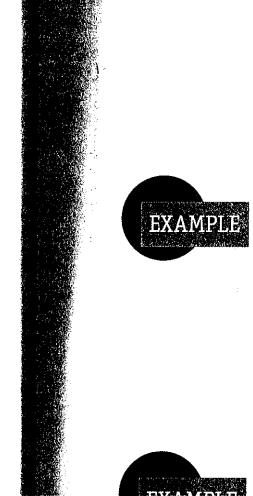
The mean tells us how large each observation in the data set would be if the total were split equally among all the observations. In the language of young children, the mean is the "fair share" value. The mean of a distribution also has a physical interpretation, as the following Activity shows.

ACTIVITY Mean as a "balance point"

MATERIALS: Foot-long ruler, pencil, and 5 pennies per group of 3 to 4 students

In this Activity, you'll investigate an interesting property of the mean.

- 1. Stack all 5 pennies above the 6-inch mark on your ruler. Place your pencil under the ruler to make a "seesaw" on a desk or table. Move the pencil until the ruler balances. What is the relationship between the location of the pencil and the mean of the five data values: 6, 6, 6, 6, 6?
- 2. Move one penny off the stack to the 8-inch mark on your ruler. Now move one other penny so that the ruler balances again without moving



tions are smaller and the other half are larger. Io find the median of a distribution:

- Arrange all observations in order of size, from smallest to largest.
- 2. If the number of observations n is odd, the median M is the center observation in the ordered list.
- 3. If the number of observations n is even, the median M is the average of the two center observations in the ordered list.

Medians require little arithmetic, so they are easy to find by hand for small sets of data. Arranging even a moderate number of values in order is tedious, however, so finding the median by hand for larger sets of data is unpleasant.

Travel Times to Work in North Carolina Finding the median when n is odd

What is the median travel time for our 15 North Carolina workers? Here are the data arranged in order:

5 10 10 10 10 12 15 20 20 25 30 30 40 40 60

The count of observations n = 15 is odd. The bold 20 is the center observation in the ordered list, with 7 observations to its left and 7 to its right. This is the median, M = 20 minutes.



A stemplot makes finding the median easy because it arranges the observations in order.

$$M = \frac{20 + 25}{2} = 22.5$$
 minutes

Interpretation: In the sample of New York workers, about half of the people reported traveling less than 22.5 minutes to work, and about half reported traveling more.



Comparing the Mean and the Median

Our discussion of travel times to work in North Carolina illustrates an important difference between the mean and the median. The median travel time (the midpoint of the distribution) is 20 minutes. The mean travel time is higher, 22.5 minutes. The mean is pulled toward the right tail of this right-skewed distribution. The median, unlike the mean, is resistant. If the longest travel time were 600 minutes rather than 60 minutes, the mean would increase to more than 58 minutes but the median would not change at all. The outlier just counts as one observation above the center, no matter how far above the center it lies. The mean uses the actual value of each observation and so will chase a single large observation upward.



You can compare the behavior of the mean and median by using the *Mean and Median* applet at the book's Web site, www.whfreeman.com/tps4e.

Comparing the Mean and Median

The mean and median of a roughly symmetric distribution are close together. If the distribution is exactly symmetric, the mean and median are exactly the same. In a skewed distribution, the mean is usually farther out in the long tail than is the median.³⁹



0005 New York worker who reported a 45-minute travel time to work.

005555

005

005

CHECK YOUR UNDERSTANDING

Ouestions 1 through 4 refer to the following setting. Here, once again, is the stemplot of travel times to work for 20 randomly selected New Yorkers. Earlier, we found that the median was 22.5 minutes.

- 1. Based only on the stemplot, would you expect the mean travel time to be less than, about the same as, or larger than the median? Why?
- 2. Use your calculator to find the mean travel time. Was your answer to Question 1 correct?
- 3. Interpret your result from Question 2 in context without using the words "mean" or "average."
- 4. Would the mean or the median be a more appropriate summary of the center of this distribution of drive times? Justify your answer.

Measuring Spread: The Interquartile Range (*IQR*)

A measure of center alone can be misleading. The mean annual temperature in San Francisco, California, is 57°F—the same as in Springfield, Missouri. But the wardrobe needed to live in these two cities is very different! That's because daily temperatures vary a lot more in Springfield than in San Francisco. A useful numerical description of a distribution requires both a measure of center and a measure of spread.

The simplest measure of variability is the range, which we defined earlier as the difference between the largest and smallest observations. The range shows the full spread of the data. But it depends on only the maximum and minimum values.

The interquartile range (IQR) is defined as

$$IQR = Q_3 - Q_1$$

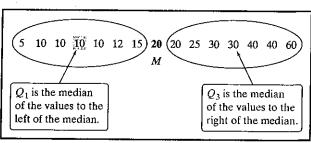
Be careful in locating the quartiles when several observations take the same numerical value. Write down all the observations, arrange them in order, and apply the rules just as if they all had distinct values.

Let's look at how this process works using a familiar set of data.

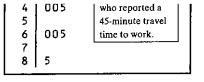


Travel Times to Work in North Carolina Calculating quartiles

Our North Carolina sample of 15 workers' travel times, arranged in increasing order, is

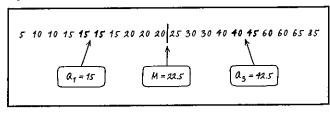


There is an odd number of observations, so the median is the middle one, the bold 20 in the list. The first quartile is the median of the 7 observations to the left of the median. This is the 4th of these 7 observations, so $Q_1 = 10$ minutes (shown in blue). The third quartile is the median of the 7 observations to the right of the



PROBLEM: Find and interpret the interquartile range (IQR).

SOLUTION: We begin by writing the travel times arranged in increasing order:



There is an even number of observations, so the median lies halfway between the middle pair. Its value is M=22.5 minutes. (We marked the location of the median by |.) The first quartile is the median of the 10 observations to the left of M=22.5. So it's the average of the two bold 15s: $\mathcal{Q}_1=15$ minutes. The third quartile is the median of the 10 observations to the right of M=22.5. It's the average of the bold numbers 40 and 45: $\mathcal{Q}_3=42.5$ minutes. The interquartile range is

$$IQR = Q_3 - Q_1 = 42.5 - 15 = 27.5$$
 minutes

Interpretation: The range of the middle half of travel times for the New Yorkers in the sample is 27.5 minutes.

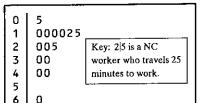


Identifying Outliers

In addition to serving as a measure of spread, the interquartile range (IQR) is used as part of a rule of thumb for identifying outliers.



Travel Times to Work in North Carolina Identifying outliers



Earlier, we noted the influence of one long travel time of 60 minutes in our sample of 15 North Carolina workers.

PROBLEM: Determine whether this value is an outlier.

SOLUTION: Earlier, we found that $Q_1 = 10$ minutes, $Q_3 = 30$ minutes, and IQR = 20 minutes. To check for outliers, we first calculate

$$1.5 \times IQR = 1.5(20) = 30$$

By the $1.5 \times IQR$ rule, any value greater than

$$Q_3 + 1.5 \times IQR = 30 + 30 = 60$$

or less than

$$Q_1 - 1.5 \times IQR = 10 - 30 = -20$$

would be classified as an outlier. The maximum value of 60 minutes is not quite large enough to be flagged as an outlier.

For Practice Try Exercise 89(b)

AP EXAMTIP You may be asked to determine whether a quantitative data set has any outliers. Be prepared to state

and use the rule for

identifying outliers.

Whenever you find outliers in your data, try to find an explanation for them. Sometimes the explanation is as simple as a typing error, like typing 10.1 as 101. Sometimes a measuring device broke down or someone gave a silly response, like the student in a class survey who claimed to study 30,000 minutes per night. (Yes, that really happened.) In all these cases, you can simply remove the outlier from your data. When outliers are "real data," like the long travel times of some

New York workers, you should choose statistical methods that are not greatly

Boxplot FX AMPLE and the median, about 25% are between the median and Q_3 , and about 25% are between Q_3 and the maximum.

The five-number summary of a distribution leads to a new graph, the boxplot (sometimes called a box and whisker plot).

How to Make a Boxplot

- A central box is drawn from the first quartile (Q_1) to the third quartile (Q_3) .
- A line in the box marks the median.
- Lines (called whiskers) extend from the box out to the smallest and largest observations that are not outliers.

Here's an example that shows how to make a boxplot.

Home Run King Making a boxplot

Barry Bonds set the major league record by hitting 73 home runs in a single season in 2001. On August 7, 2007, Bonds hit his 756th career home run, which broke Hank Aaron's longstanding record of 755. By the end of the 2007 season

broke Hank Aaron's longstanding record of 755. By the end of the 2007 season when Bonds retired, he had increased the total to 762. Here are data on the number of home runs that Bonds hit in each of his 21 complete seasons:

16 25 24 19 33 25 34 46 37 33 42 40 37 34 49 73 46 45 45 26 28

PROBLEM: We want to make a boxplot for these data.

North Carolina New York FIGURE 1.19 Boxplots comparing the travel times to work of samples of workers in North Carolina and New York.

Shape: We see from the graph that both distributions are right-skewed. For both states, the distance from the minimum to the median is much smaller than the distance from the median to the maximum.

Center: It appears that travel times to work are generally a bit longer in New York

comparison, For the travel time to work data:

than in North Carolina. The median, both quartiles, and the maximum are all larger in New York.

Spread: Travel times are also more variable in New York, as shown by the heights

of the boxes (the *IQR*) and the spread from smallest to largest time.

Outliers: Earlier, we showed that the maximum travel time of 85 minutes is an outlier for the New York data. There are no outliers in the North Carolina sample.

The following Activity reinforces the important ideas of working with boxplots.⁴⁰

ACTIVITY Do you know your geography?

mountain chains? The populations of states and cities? In this Activity, you'll have a chance to demonstrate your geographic knowledge by estimating the population of a capital city.

1. Your teacher will give each student a slip of paper with two questions about the population of a U.S. capital city. Look only at your paper. Answer the

How well do you know the U.S. state capitals? The locations of major rivers and

- questions to the best of your ability.

 2. Now your teacher will share the details of what was on the slips of paper. About half the students in the class received one version of the first question, and the other half received a different version. The second question was the same on all the slips.
- and the other half received a different version. The second question was the same on all the slips.

 3. Students in the class should divide into two groups based on which version of the first question they received. Within each group, line up in order of your

4. Draw a boxplot of the data.

TECHNOLOGY CORNER Making calculator boxplots

The TI-83/84 and TI-89 can plot up to three boxplots in the same viewing window. Let's use the calculator to make side-by-side boxplots of the travel time to work data for the samples from North Carolina and New York.

- 1. Enter the travel time data for North Carolina in L1/list1 and for New York in L2/list2.
- 2. Set up two statistics plots: Plot1 to show a boxplot of the North Carolina data and Plot2 to show a boxplot of the New York data.

TI-83/84



T**I-**89



Note: The calculator offers two types of boxplots: a "modified" boxplot that shows outliers and a standard boxplot that doesn't. We'll always use the modified boxplot.

3. Use the calculator's Zoom feature to display the side-by-side boxplots. Then Trace to view the five-number summary.

TI-83/84

TI-89







The five-number summary is not the most common numerical description of a distribution. That distinction belongs to the combination of the mean to measure center and the *standard deviation* to measure spread. The standard deviation and its close relative, the *variance*, measure spread by looking at how far the observations are from their mean. Let's explore this idea using a simple set of data.



How Many Pets?

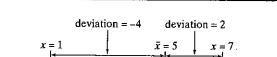
Investigating spread around the mean

In the Think About It on page 52, we examined data on the number of pets owned by a group of 9 children. Here are the data again, arranged from lowest to highest:

3 4 4 4 5 7 8 9

Earlier, we found the mean number of pets to be $\bar{x} = 5$. Let's look at where the observations in the data set are relative to the mean.

Figure 1.20 displays the data in a dotplot, with the mean clearly marked. The data value 1 is 4 units below the mean. We say that its *deviation* from the mean is -4. What about the data value 7? Its deviation



is 7 - 5 = 2 (it is 2 units above the mean). The arrows in the figure mark these two deviations from the mean. The deviations show how much the data

$$5 5-5=0 0^2=0$$

$$7 7-5=2 2^2=4$$

$$8 8-5=3 3^2=9$$

$$9 9-5=4 4^2=16$$

$$sum=?? sum=??$$

We have added a column to the table that shows the square of each deviation $(x_i - \overline{x})^2$. Add up the squared deviations. Did you get 52? Now we compute the average squared deviation—sort of. Instead of dividing by the number of observations n, we divide by n - 1:

"average" squared deviation =
$$\frac{16+4+1+1+1+0+4+9+16}{9-1} = \frac{52}{8} = 6.5$$

This value, 6.5, is called the variance.

Because we squared all the deviations, our units are in "squared pets." That's no good. We'll take the square root to get back to the correct units—pets. The resulting value is the **standard deviation**:

standard deviation =
$$\sqrt{\text{"average" squared deviation}} = \sqrt{6.5} = 2.55$$

This 2.55 is roughly the average distance of the values in the data set from the mean.

As you can see, the average distance in the standard deviation is found in a rather unexpected way. Why do we divide by n-1 instead of n when calculating the variance and standard deviation? The answer is complicated but will be revealed in Chapter 7.

 s_x is the square root of this average squared distance:

$$s_x = \sqrt{\frac{1}{n-1} \sum (x_i - \overline{x})^2}$$

Many calculators report two standard deviations, giving you a choice of dividing by n or by n-1. The former is usually labeled σ_x , the symbol for the standard deviation of a population. If your data set consists of the entire population, then it's appropriate to use σ_x . More often, the data we're examining come from a sample. In that case, we should use s_x .

More important than the details of calculating s_x are the properties that determine the usefulness of the standard deviation:

- s_x measures *spread about the mean* and should be used only when the mean is chosen as the measure of center.
- s_x is always greater than or equal to 0. $s_x = 0$ only when there is no variability. This happens only when all observations have the same value. Otherwise, $s_x > 0$. As the observations become more spread out about their mean, s_x gets larger.
- s_x has the same units of measurement as the original observations. For example, if you measure metabolic rates in calories, both the mean \bar{x} and the standard deviation s_x are also in calories. This is one reason to prefer s_x to the variance s_x^2 , which is in squared calories.
- Like the mean \bar{x} , s_x is not resistant. A few outliers can make s_x very large.

The use of squared deviations makes s_x even more sensitive than \bar{x} to a few extreme observations. For example, the standard deviation of the travel times for the 15 North Carolina workers is 15.23 minutes. If we omit the maximum value of 60 minutes, the standard deviation drops to 11.56 minutes.

New York workers from the previous Technology Corner (page 61). We'll start by showing you the necessary calculator techniques and then look at output from computer software. I. One-variable statistics on the calculator If you haven't done so already, enter the North Carolina data in L1/list1 and the New York data in L2/list2. 1. Find the summary statistics for the North Carolina travel times. TI-83/84 TI-89 • Press STAT ▶ (CALC); • Press F4 (Calc); choose choose 1:1-VarStats. 1:1-Var Stats. • Press ENTER, Now press 2nd 1 (L1) • Type list! in the list box. and ENTER. Press ENTER Press volume to see the rest of the one-variable statistics for North Carolina. Stats .46666667

2. Repeat Step 1 using L2/list2 to find the summary statistics for the New York



II. Output from statistical software We used Minitab statistical software to produce descriptive statistics for the New York and North Carolina travel time data. Minitab allows you to choose which numerical summaries are included in the output.

Descriptive Statistics: Travel time to work

We now have a choice between two descriptions of the center and spread of a distribution: the median and IQR, or \bar{x} and s_x . Because \bar{x} and s_x are sensitive to extreme observations, they can be misleading when a distribution is strongly skewed or has outliers. In these cases, the median and IQR, which are both resistant to extreme values, provide a better summary. We'll see in the next chapter that the mean and standard deviation are the natural measures of center and spread for a very important class of symmetric distributions, the Normal distributions.

Choosing Measures of Center and Spread

The median and IQR are usually better than the mean and standard deviation for describing a skewed distribution or a distribution with strong outliers. Use \bar{x} and s_x only for reasonably symmetric distributions that don't have outliers.

Remember that a graph gives the best overall picture of a distribution. Numerical measures of center and spread report specific facts about a distribution, but they do not describe its entire shape. Numerical summaries do not highlight the presence of multiple peaks or clusters, for example. Always plot your data.

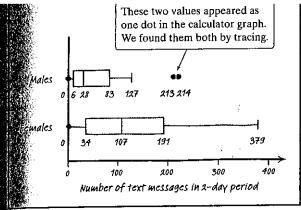
Here's a final example that shows the thinking involved in choosing measures of center and spread when comparing two sets of quantitative data.



Who Texts More—Males or Females?
Pulling it all together



For their final project, a group of AP Statistics students investigated their belief



oxplots of the texting data.

FIGURE 1.21 Side-by-side

instead of the mean and standard deviation when discussing center and spread. Shape: Both distributions are heavily right-skewed. Center: On average, females text more than males. The median number of texts for females (107) is about four times as high as for males (28). In fact, the median for the females is above the third quartile for the males. This indicates that over 75% of the males texted less than the "typical" (median) female. Spread: There is much more variability in texting among the females than the males. The IQR for females (157) is about twice the IQR for males (77). Outliers: There are two outliers in the male distribution: students who reported 213 and 214 texts in two days. The female distribution has no outliers.

For Practice Try Exercise 105

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CONCLUDE: The data from this survey project give very strong evidence to support the students' belief that females text more than males. Females sent and received a median of 107 texts over the two-day period, which exceeded the number of texts reported by over 75% of the males.

AP EXAMTIP Use statistical terms carefully and correctly on the AP exam. Don't say "mean" if you really mean "median." Range is a single number; so are Q_1 , Q_3 , and IQR. Avoid colloquial use of language, like "the outlier skews the mean." Skewed is a shape. If you misuse a term, expect to

lose some credit.

Now it's time for you to put what you have learned into practice in the following Data Exploration.

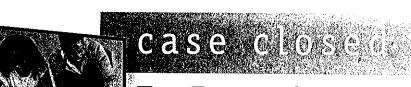
DATA EXPLORATION Did Mr. Starnes stack his class?

Mr. Starnes teaches AP Statistics, but he also does the class scheduling for the
 high school. There are two AP Statistics classes—one taught by Mr. Starnes and

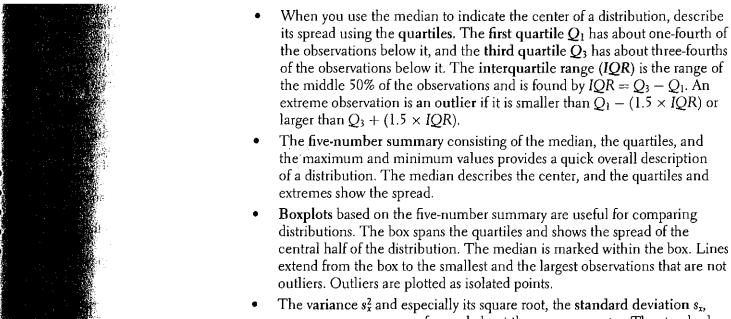
	3.085	570	2.9	502.5
	3.75	710	3.95	640
	3.4	630	3.1	630
	3.338	630	2.85	580
	3.56	670	2.9	590
	3.8	650	3.245	600
	3.2	660	3.0	600
	3.1	510	3.0	620
			2.8	580
			2.9	600
***************************************			3.2	600

Did Mr. Starnes stack his class? Give appropriate graphical and numerical

At the end of each chapter, we'll return to the chapter-opening Case Study to let you know what happened. We call this feature "Case Closed!"



evidence to support your conclusion.



- its spread using the quartiles. The first quartile Q_1 has about one-fourth of the observations below it, and the third quartile Q_3 has about three-fourths of the observations below it. The interquartile range (IQR) is the range of the middle 50% of the observations and is found by $IQR = Q_3 - Q_1$. An extreme observation is an outlier if it is smaller than $Q_1 - (1.5 \times IQR)$ or larger than $Q_3 + (1.5 \times IQR)$. The five-number summary consisting of the median, the quartiles, and
- the maximum and minimum values provides a quick overall description of a distribution. The median describes the center, and the quartiles and extremes show the spread. Boxplots based on the five-number summary are useful for comparing distributions. The box spans the quartiles and shows the spread of the
 - extend from the box to the smallest and the largest observations that are not outliers. Outliers are plotted as isolated points. The variance s_x^2 and especially its square root, the standard deviation s_x are common measures of spread about the mean as center. The standard
- deviation s_x is zero when there is no variability and gets larger as the spread increases. The median is a resistant measure of center because it is relatively
- unaffected by extreme observations. The mean is nonresistant. Among measures of spread, the *IQR* is resistant, but the standard deviation is not. The mean and standard deviation are good descriptions for symmetric
- distributions without outliers. They are most useful for the Normal distributions introduced in the next chapter. The median and IQR are a better description for skewed distributions.
- Numerical summaries do not fully describe the shape of a distribution. Always blot your data

86 84 91 /5 /6 00 /1
87 76 96 82 90 98 93

Calculate the mean. Show your work. Interpret your result in context.

80. Cowboys The 2009 roster of the Dallas Cowboys professional football team included 7 defensive linemen. Their weights (in pounds) were 306, 305, 315, 203, 218, 300, and 285. Calculate the mean. Show

professional football team included 7 detersive into men. Their weights (in pounds) were 306, 305, 315, 303, 318, 309, and 285. Calculate the mean. Show your work. Interpret your result in context.

81. Quiz grades Refer to Exercise 79.

(a) Find the median by hand. Show your work.

pg 53

- (a) Find the median by hand. Show your work.
 Interpret your result in context.
 (b) Suppose Joey has an unexcused absence for the 15th quiz, and he receives a score of zero. Recalculat
- 15th quiz, and he receives a score of zero. Recalculate the mean and the median. What property of measures of center does this illustrate?
- 82. Cowboys Refer to Exercise 80.(a) Find the median by hand. Show your work.
 - Interpret your result in context.

 (b) Suppose the lightest lineman had weighed 265 pounds instead of 285 pounds. How would this change affect the mean and the median? What property of measures of center does this illustrate?
- 83. Incomes of college grads According to the Census Bureau, the mean and median 2008 income of people at least 25 years old who had a bachelor's

\$50,000 each, and the firm's owner \$270,000. What is the mean salary paid at this firm? How many of the employees earn less than the mean? What is the median salary? Write a sentence to describe how an unethical recruiter could use statistics to mislead prospective employees.

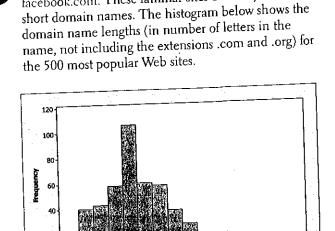
each of its five clerks \$22,000, two junior accountants

prospective employees.

87. Domain names When it comes to Internet domain names, is shorter better? According to one ranking of Web sites in 2008, the top 8 sites (by number of "hits") were yahoo.com, google.com, youtube.com,

live.com, msn.com, myspace.com, wikipedia.org, and

facebook.com. These familiar sites certainly have



degree but no higher degree were \$48,097 and

Servings of fruit per day

- (a) With a little care, you can find the median and the quartiles from the histogram. What are these numbers? How did you find them?
- (Б) Estimate the mean of the distribution. Explain

Quiz grades Refer to Exercise 79.

- (a) Find and interpret the interquartile range (IQR).
- (b) Determine whether there are any outliers. Show your work.

Occowboys Refer to Exercise 80.

- (a) Find and interpret the interquartile range (IQR).
- (b) Determine whether there are any outliers. Show your work.

Don't call me In a September 28, 2008, article titled "Letting Our Fingers Do the Talking," the New York Times reported that Americans now send more text messages than they make phone calls. According to a study by Nielsen Mobile, "Teenagers ages 13 to 17 are by far the most prolific texters, sending or receiving 1,742 messages a month." Mr. Williams, a

high school statistics teacher, was skeptical about the

claims in the article. So he collected data from his

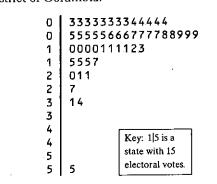
first-period statistics class on the number of text messages and calls they had sent or received in the

past 24 hours. Here are the texting data:

7 1 29 25 8 5 1 25 98 9 0 26

(a) Make a boxplot of these data by hand. Be sure to

- -20 0 20 40 60 80 100 120 Difference (texts – calls)
- (a) Do these data support the claim in the article about texting versus calling? Justify your answer with appropriate evidence.
- (b) Can we draw any conclusion about the preferences of all students in the school based on the data from Mr. Williams's statistics class? Why or why not?
- 94. Electoral votes To become president of the United States, a candidate does not have to receive a majority of the popular vote. The candidate does have to win a majority of the 538 electoral votes that are cast in the Electoral College. Here is a stemplot of the number of electoral votes for each of the 50 states and the District of Columbia.



(a) Make a boxplot of these data by hand. Be sure to

(a) Read the graph: about what were the highest and lowest daily returns on the stock fund?

- (b) Read the graph: the median return was about the same on both investments. About what was the median return?
- (c) What is the most important difference between the two distributions?
- 96. Income and education level Each March, the Bureau of Labor Statistics compiles an Annual Demographic Supplement to its monthly Current Population Survey.44 Data on about 71,067 individuals between the ages of 25 and 64 who were employed full-time were collected in one of these surveys. The boxplots below compare the distributions of income for people with five levels of education. This figure is a variation of the boxplot idea: because large data sets often contain very extreme observations, we omitted the individuals in each category with the top 5% and bottom 5% of incomes. Write a brief description of how the distribution of income changes with the highest level of education reached. Give specifics from the graphs to support your statements.

- variance and the standard deviation.
- (b) Interpret the value of s_x you obtained in (a).
- 98. Feeling sleepy? The first four students to arrive for a first-period statistics class were asked how much sleep (to the nearest hour) they got last night. Their responses were 7, 7, 9, and 9.
 - (a) Find the standard deviation from its definition. That is, find the deviations of each observation from the mean, square the deviations, then obtain the variance and the standard deviation.
- (b) Interpret the value of s_x you obtained in (a).
 (c) Do you think it's safe to conclude that the meaning of the concluder that the concluder
- (c) Do you think it's safe to conclude that the mean amount of sleep for all 30 students in this class is close to 8 hours? Why or why not?
- 99. Shopping spree The figure displays computer output from Data Desk for data on the amount spent by 50 grocery shoppers.

Hamel

300

tion would you guess has a more symmetrical shape?

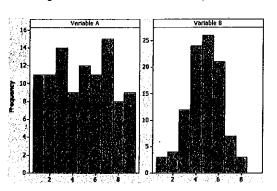
Explain.

(b) Explain how the IQRs of these two distributions can be so similar even though the standard deviation

can be so similar even though the standard deviations are quite different.

(c) Does it appear that males perform more C-sections? Justify your answer.

- 101. The *IQR* Is the interquartile range a resistant measure of spread? Give an example of a small data set that supports your answer.
- 102. Measuring spread Which of the distributions shown has a larger standard deviation? Justify your answer.



- 103. SD contest This is a standard deviation contest. You must choose four numbers from the whole numbers 0 to 10, with repeats allowed.
 - (a) Choose four numbers that have the smallest possible standard deviation.

(b) Choose four numbers that have the largest pos-

Do these data support the belief that women have better study habits and attitudes toward learning than men? (Note that high scores indicate good study habits and attitudes toward learning.) Follow the four-step process.

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from Amherst College studied the relationship between varieties of the tropical flower Heliconia on the island of Dominica and the different species of hummingbirds that fertilize the flowers. 45 Over time, the researchers believe, the lengths of the flowers and the forms of the hummingbirds' beaks have evolved to match each other. If that is true, flower varieties fertilized by different hummingbird species should

have distinct distributions of length.

The table below gives length measurements (in millimeters) for samples of three varieties of *Heliconia*, each fertilized by a different species of hummingbird. Do these data support the researchers' belief? Follow the four-step process.

H. bihai

47.12	46.75	46:80	47.12	46:67	47.43	46:44	46.64
40.07	40.04	40.45	50.00	E0 10	40.047	40.04	40.06

H. caribaea red

41.90	42.01	41.93	43.09	41.47	41.69	39.78	40.57

39.63	42.18	40.66	37.87	39.16	37.40	38,20	38.07
38.10	37:97	38.79 -	38.23	38.87	37.78	38:01	

(a) Median (d) Range (b) Mean (e) Maximum 181 171.5 160 (c) Standard deviation 157.5 145.5 156 182 168.5 177 162.5 160.5 185.5 110. What are all the values that a standard deviation s_x Make an appropriate graph to display these data. can possibly take? Describe the shape, center, and spread of the distribu-(a) $s_x \ge 0$ (d) $-1 \le s_r \le 1$ tion. Are there any outliers? (b) $s_r > 0$ (e) Any number (c) $0 \le s_x \le 1$ 113. Success in college (1.1) The 2007 Freshman Survey asked first-year college students about their "habits of Exercises 111 and 112 refer to the following setting. mind"-specific behaviors that college faculty have We used CensusAtSchool's "Random Data Selector" to identified as being important for student success. One choose a sample of 50 Canadian students who completed question asked students, "How often in the past year a survey in 2007-2008. did you revise your papers to improve your writing?" Another asked, "How often in the past year did you 30 seek feedback on your academic work?" The figure is a bar graph comparing male and female responses to 25 method of communication these two questions.46 20 Male Female 15 -100 10 80 "Frequently" 5 60 54.9% Internet that of Men MyStatelfteedood 36.9% 37.6% 40 -20 Revise papers to Method of communication improve writing

190

101 1/1

168.5

49.0%

182

165

167

187

mgn oddier is added to your data?